

Navigating Stormy Waters: Crises, Selection and Productivity Dynamics Under Financial Frictions

Ufuk Akcigit
UChicago

Harun Alp
FRB

Ege Y. Ercan
Stanford GSB

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Motivation

- Firms grow by borrowing and investing in risky projects to enhance their productivity.
- Research Questions
 - How do financial conditions affect firm dynamics and productivity growth?
 - How do firm heterogeneities interact with financials?

What We Do

- Build a GE model of firm dynamics with
 - Endogenous productivity growth
 - Rich firm heterogeneity (types)
 - Crucial to match both size and age moments
 - Firms relying borrowing under financial frictions
 - default decision
 - endogenous interest rate
 - endogenous borrowing constraints

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- Calibrate the model with micro data on US firms.
- Study productivity dynamics under a “crisis” shock.

Preview of Results

- Firm **heterogeneity** is important in evolution of crises.
 - Crises hit harder but recovery is faster under heterogeneity.
 - It determines the extend of reallocation through bankruptcy.
- Efficiency of the **bankruptcy process** is also critical in crises.
 - If the bankruptcy process did not result in reallocation, the economy would not bounce back from the crisis.
- **Uniform stabilization policies** can depress long-term recovery.

Literature Review

Financial Frictions and Firm Dynamics:

- Jermann and Quadrini (2012), Cooley and Quadrini (2001), Miao (2005), Li et al. (2016)

Financial Frictions and Endogenous Growth:

- Malamud and Zucchi (2019), Laeven et al. (2020), Chatterjee and Eyigungor (2020), Geelen et al. (2020)

MODEL

Market Structure

- The household consumes some final good, Y , aggregated with technology:

$$\ln(Y) = \int_{\mathcal{N}} \ln(y_j) dj, \quad (1)$$

- Each intermediate good is produced by one firm.

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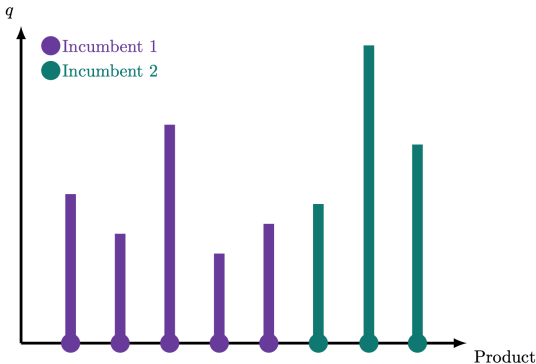
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where q_j is the productivity and l_j is the labor hired.

- A firm is a collection of production lines (Klette and Kortum, 2004)
 - Investment to capture other product lines by improving their productivity.
 - Shrinks due to other firms' investment.

Snapshot of Competition I

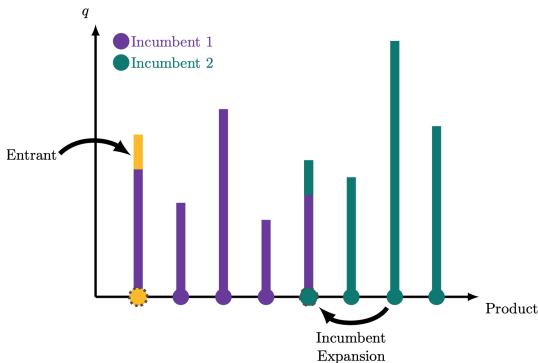
Figure 1: Before



- Two incumbents with cutting edge technology in 8 products.

Snapshot of Competition II

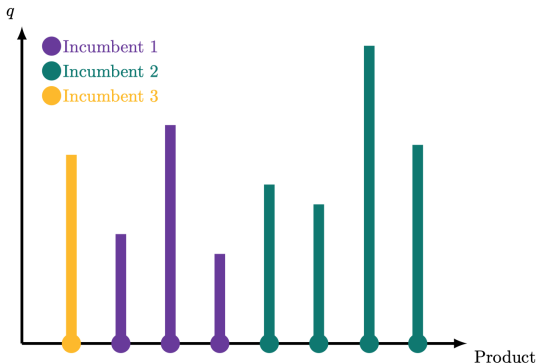
Figure 2: During



- Both **entrant** and **incumbent 2** innovate over **incumbent 1**.
- That is, **incumbent 1** loses two product lines.
- New technologies in these lines are **more productive**.

Snapshot of Competition III

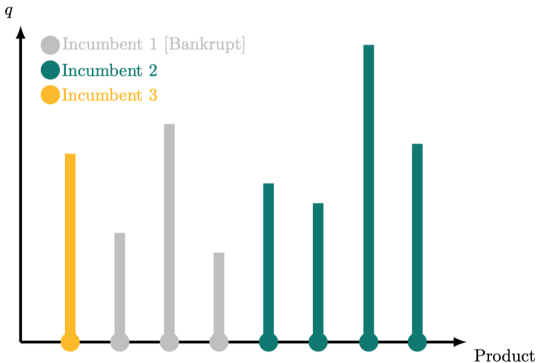
Figure 3: After (Solvent)



- After **turnover**, there are **three incumbents**.

Snapshot of Competition IV

Figure 4: After (Insolvent)



- Sudden contraction can lead **incumbent 1** to **bankruptcy**.
- **Reallocation** of **bankrupt technologies** will be important.

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1) Size, $n \in \mathbb{N}$ (i.e., number of product lines)

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3) Debt $D \in \mathbb{R}$:

- Financing with defaultable short-term debt instrument
- Heterogenous endogenous debt limits and interest rate spreads.

Investments and Productivity

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Investments Cost Function:

- Productivity flow rate $xn \geq 0$ costs

$$C(x) = \frac{1}{\theta_k} x^\eta n Y. \quad (2)$$

where $\eta > 1$ is the inverse innovation elasticity.

- Undirected search for better technology.
- W/ arrival rate $xn \geq 0$, firm discovers a better technology.

Firm Financials

1) Law of Motion for Debt:

$$\dot{D} = \varphi(p) - \underbrace{(1 - \tau_{tax}) [\pi n - c(x, \theta_k) - R(D, n, k)D]}_{\text{Before-Tax Net Income}}, \quad (3)$$

where

$$R(D, n, k) = r + \underbrace{\delta(D, n, k)}_{\text{spread}} \quad (4)$$

coming from the bank's problem and p is payout.

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- Firm exits when it loses all its product line (competition).
- At the rate $\varepsilon > 0$, the firm exits exogenously.

Bank's Problem

- Competitive banks offering firm-specific loan menus:
 - Endogenous firm-specific interest spreads, $\delta(D, n, k)$.
 - Endogenous firm-specific debt limits, $\bar{D}(n, k)$.

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 - Banks resell them at a discount.
 - Bankruptcy process is resolved after some delay (ψ).
 - No investment during the process.

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 - **Source of reallocation**
 - New firm has a lower debt.
 - New firm may have a higher growth potential (θ_k).

Incumbent's Value Function

$$\begin{aligned}
 rV(D, n, k) = \max \left\{ 0, \max_{x,p} \left\{ pnY \right. \right. \\
 + \frac{\partial V}{\partial D}(D, n, k) \dot{D}(x, p; D, n, k) \\
 + xn [V(D, n + 1, k) - V(D, n, k)] \\
 + \tau n [V(D, n - 1, k) - V(D, n, k)] \\
 + 1_{k=H} \phi_{H \rightarrow L} [V(D, n, L) - V(D, n, H)] \\
 - \varepsilon V(D, n, k) \\
 \left. \left. + \partial_t [V(D, n, k)] \right\} \right\},
 \end{aligned}$$

s.t.

$$\bar{D}(n, k) \geq D.$$

CALIBRATION

Set-Up

- We calibrate the model to the US.
- 12 internally calibrated parameters with 17 moments calculated with "Federal Reserve Y-14" data and one moment calculated with Compustat.

Loss Function

$$\sum_{i=1}^{12} \frac{w(i) |\text{model}(i) - \text{data}(i)|}{\frac{1}{2} |\text{model}(i)| + \frac{1}{2} |\text{data}(i)|}, \quad (6)$$

where $w(i)$ is the i th moment's weight.

Data

- Supervisory FR Y-14 dataset (2013-2019)
 - Financial information for US firms
 - Not only public firms but also a large number of small and mid-sized private businesses.
 - More than 600,000 firm×year observations, around 190,000 unique firms.
 - Represent almost 80 percent of the US aggregate output (public firms account only around 40 percent).
- Compustat.
 - Payout information for large firms.

Fit

Table 1: Moments

#	Moment	Data	Model
1	Payout Mean (+, Very Large)	0.081	0.061
2	Interest Spread (Small Size-Low Leverage)	0.014	0.012
3	Interest Spread (Small Size-High Leverage)	0.018	0.023
4	Interest Spread (Large Size-Low Leverage)	0.013	0.012
5	Interest Spread (Large Size-High Leverage)	0.015	0.018
6	Default Rate (Small Size-Low Leverage)	0.026	0.047
7	Default Rate (Small Size-High Leverage)	0.049	0.061
8	Default Rate (Large Size-Low Leverage)	0.018	0.007
9	Default Rate (Large Size-High Leverage)	0.030	0.049
10	Leverage (Small Size-Low Leverage)	0.090	0.130
11	Leverage (Small Size-High Leverage)	1.540	1.502
12	Leverage (Large Size-Low Leverage)	0.097	0.161
13	Leverage (Large Size-High Leverage)	0.997	0.945
14	Growth (Small Size-Low Leverage)	0.050	0.048
15	Growth (Small Size-High Leverage)	0.148	0.116
16	Growth (Large Size-Low Leverage)	-0.000	-0.001
17	Growth (Large Size-High Leverage)	0.019	0.009
18	Aggregate Growth	0.022	0.022

*Large/Small firms are divided w.r.t. the median size.

**High/Low leverage firms are divided w.r.t. the median leverage, defined as debt to sales ratio.

***Very Large firms are the top 10% by size.

Parameters

Table 2: External Calibration

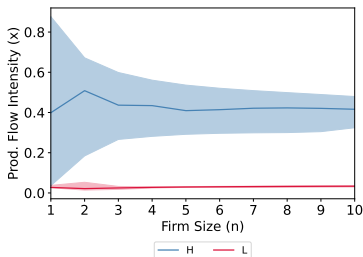
#	Parameter	Description	Value
1	ρ	Discount Rate	0.02
2	ϑ	Inverse Intertemp. Elas. of Subs.	2.00
3	η	Inverse Innovation Elasticity	2.00
4	τ_{tax}	Tax Rate	0.35
5	ψ	Default Resolution Rate	0.46

Table 3: Internal Calibration

#	Parameter	Description	Value
1	κ	Payout Penalty Scale	3.605
2	χ	Fixed Cost	0.246
3	μ_0	Fixed Recovery	2.735
4	ξ	Buyer's Leverage	0.247
5	ν_0	Banking Costs	0.012
6	θ_H	H-Type Innovation Productivity	0.387
7	θ_L	L-Type Innovation Productivity	0.032
8	θ_E	Entrant Innovation Productivity	0.015
9	λ	Innovation Step Size	1.287
10	α	Share of H-Types in Entry	0.500
11	$\phi_{H \rightarrow L}$	Transition Rate into L-Type	0.267
12	ε	Death Shock	0.002

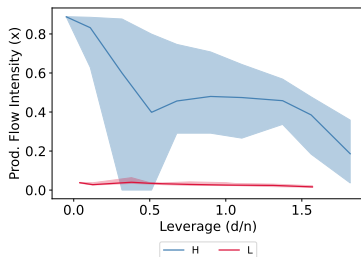
Investment by Firm Size and Leverage

(a) Investment Across Size



*Shaded regions represent middle 90% of distributions

(b) Investment Across Leverage



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- Healthy heterogeneity in investments across size, type, and leverage.
- With debt accumulation, investments start falling again (debt overhang).

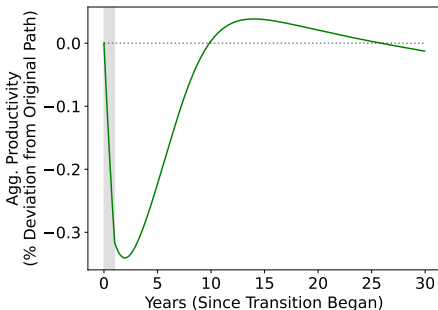
CRISIS

Crisis

- **Unanticipated Shock:** A zero probability event that occurs unexpectedly, but once it occurs, transition evolves deterministically.
- **Duration and Magnitude:** 33% decrease in gross profit margin for one year.
- **What we study:**
 - Effects of Bankruptcy on Reallocation
 - Effects of Firm Heterogeneity
 - Effects of Stabilization Policies

Productivity Loss

Figure 6: Deviation from Original Path



- Decline in productivity growth attributable to:
 - Mass bankruptcies.
 - Difficulty in expending resources on investments during crises.
 - Diminished value of expanding to new products.

Survival and Leverage

Figure 7: Survival

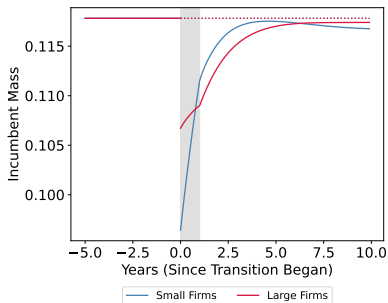
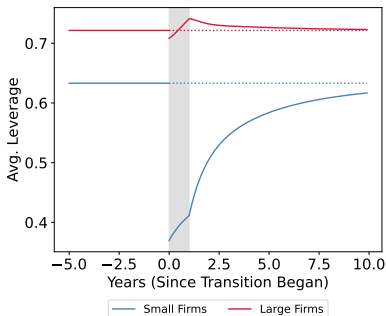


Figure 8: Leverage



- Small firms are driven into bankruptcy in large volumes.
- In the wake of bankruptcies, surviving small firms are less levered due to **rising interest rates** and **decreasing debt limits**.

Incumbent Investments

Figure 9: Incumbent Investment

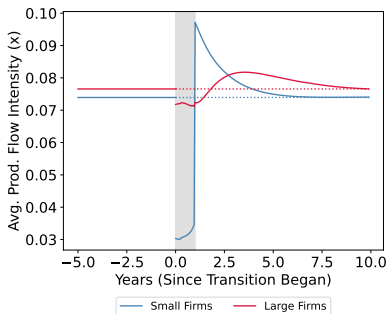
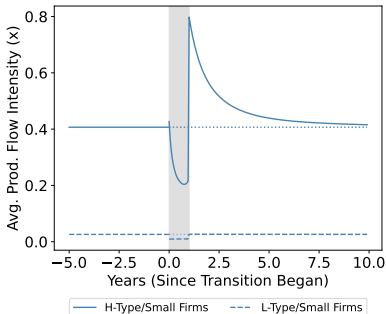


Figure 10: By Type



- L Reduction in small firm's investments cause the initial dip.
- L **Composition Effect**: Small low types are acquired by new high-type entrepreneurs on average. Recovery is fueled by small firms.
- R Within small firms, high-type firms bolster growth.

Bankruptcies and Rebound

Figure 11: Growth Decomposition

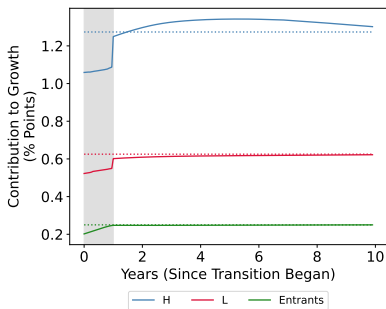
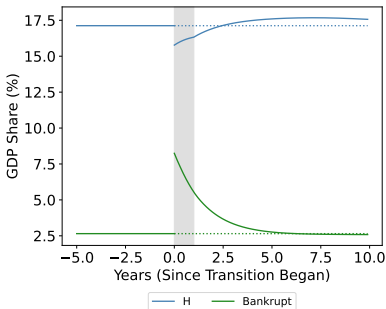


Figure 12: Selection

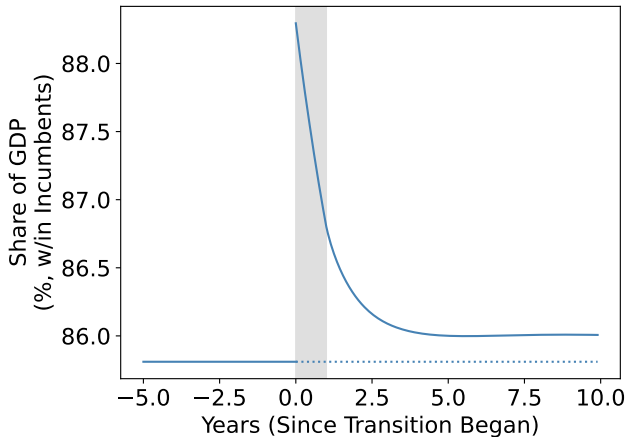


L Low-types tend to go bankrupt more.

R Recovery is driven by high-types born out of bankruptcies.

Concentration

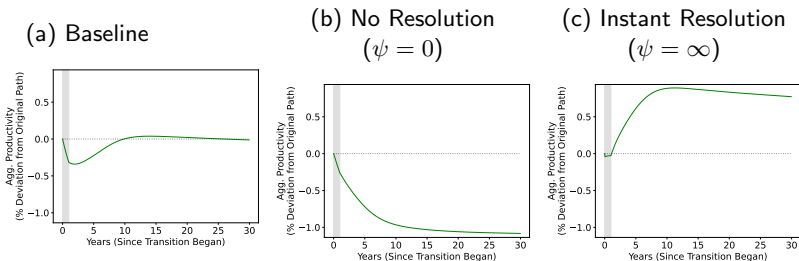
Figure 13: Top 50%



- Default of small firms lead to greater market concentration.

Bankruptcy Reallocation I

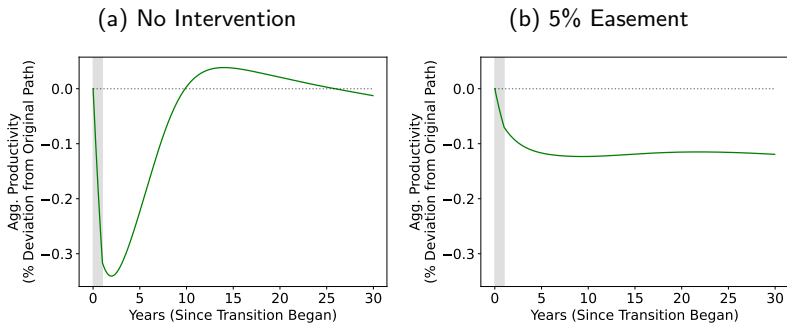
Figure 14: Productivity and Reallocation



- W/out active reallocation, productivity is permanently slashed.
- Speed of resolution can have profound effects during crises.

Stabilization Policies I

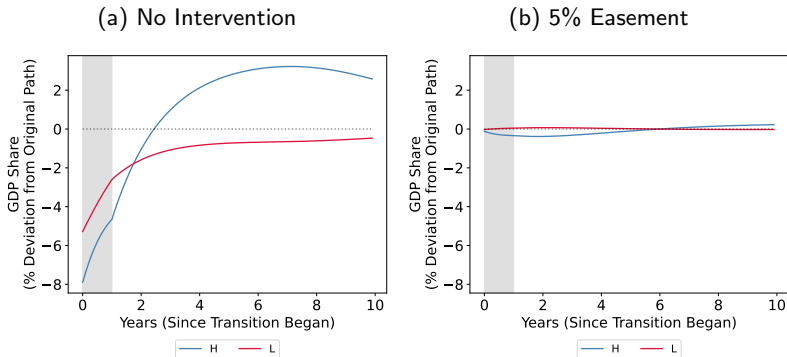
Figure 16: Productivity and Interest Rate Spreads



- Stabilization can couch the economy in the short-run.
- But, it may rob the economy of its robust recovery.

Stabilization Policies II

Figure 18: Selection and Interest Rate Spreads



- Over stabilization kills positive selection by preventing the bankruptcy of weaker (low-type) firms.

Conclusion

- Heterogeneity of the economy is important during crises.
- Efficiency of the bankruptcy process is also critical.
- Debt can cause mass bankruptcies.
- Stabilization policies can depress long-term recoveries.
- Stabilization is more important when the bankruptcy process is ineffective.